

Name _____

Key

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Determine whether the given quadratic function has a minimum value or maximum value. Then find the coordinates of the minimum or maximum point.

1) $f(x) = 5x^2 - 10x$

A) maximum; $(1, -5)$

C) minimum; $(-1, -5)$

$x = \frac{-b}{2a} = \frac{-(-10)}{2(5)} = 1$

B) maximum; $(-1, -5)$

D) minimum; $(1, -5)$

1) D

Find the coordinates of the vertex for the parabola defined by the given quadratic function.

2) $f(x) = -x^2 + 10x - 2$

A) $(5, 23)$

B) $(-5, -27)$

$x = \frac{-b}{2a} = \frac{-(10)}{2(-1)} = 5$

C) $(-5, -77)$

D) $(10, -2)$

2) A

Find the range of the quadratic function.

3) $f(x) = (x + 9)^2 - 2$

A) $[-9, \infty)$

B) $(-\infty, -2]$

C) $(-\infty, -9]$

D) $[-2, \infty)$

3) D

4) $f(x) = 11(x - 3)^2 + 5$

A) $[5, \infty)$

B) $[-5, \infty)$

C) $(-\infty, 5]$

D) $[3, \infty)$

4) A

Find the x-intercepts (if any) for the graph of the quadratic function.

5) $f(x) = 2x^2 + 10x - 48$

A) $(3, 0)$ and $(-8, 0)$

C) $(-3, 0)$ and $(-8, 0)$

$2(x^2 + 5x - 24)$
 $2(x + 8)(x - 3)$
 $x = -8, 3$

B) $(-3, 0)$ and $(8, 0)$

D) $(3, 0)$ and $(8, 0)$

5) A

6) $f(x) = x^2 + 14x + 35$ Give your answers in exact form.

A) $(-7 \pm \sqrt{14}, 0)$

B) $(7 \pm \sqrt{14}, 0)$

C) $(7 \pm \sqrt{35}, 0)$

D) $(-14 \pm \sqrt{35}, 0)$

$x = \frac{-14 \pm \sqrt{14^2 - 4(1)(35)}}{2(1)}$

$= \frac{-14 \pm \sqrt{196 - 140}}{2} = \frac{-14 \pm \sqrt{56}}{2} = \frac{-14 \pm 2\sqrt{14}}{2} = -7 \pm \sqrt{14}$

6) A

Find the y-intercept for the graph of the quadratic function.

7) $f(x) = x^2 + 5x - 6$

A) $(0, 6)$

B) $(0, 5)$

C) $(0, -6)$

D) $(0, 3)$

7) C

8) $f(x) = -x^2 + 2x + 3$

A) $(0, -3)$

B) $(3, 0)$

C) $(0, -1)$

D) $(0, 3)$

8) D

Find the domain and range of the quadratic function whose graph is described.

9) The vertex is $(1, 0)$ and the graph opens down.

A) Domain: $(-\infty, \infty)$

Range: $[0, \infty)$

C) Domain: $(-\infty, \infty)$

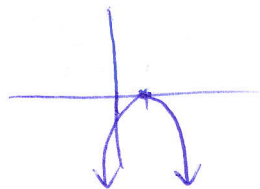
Range: $(-\infty, 1]$

B) Domain: $(-\infty, 1]$

Range: $(-\infty, 0]$

D) Domain: $(-\infty, \infty)$

Range: $(-\infty, 0]$



9) D

Use the Leading Coefficient Test to determine the end behavior of the polynomial function.

10) $f(x) = 2x^4 - 3x^3 + 3x^2 + 5x - 2$

- A) falls to the left and falls to the right
 C) rises to the left and rises to the right



- B) falls to the left and rises to the right
 D) rises to the left and falls to the right

10) C

11) $f(x) = x^3 + 2x^2 - 4x - 2$

- A) rises to the left and falls to the right
 C) falls to the left and rises to the right



- B) rises to the left and rises to the right
 D) falls to the left and falls to the right

11) C

Find the zeros of the polynomial function.

12) $f(x) = x^3 + x^2 - 6x$

A) $x = -3, x = 2$

C) $x = 0, x = -3, x = 2$

$x(x^2 + x - 6)$

$x(x+3)(x-2) = 0$

$x = 0, -3, 2$

B) $x = 0, x = 1, x = 2$

D) $x = 1, x = 2$

12) C

13) $f(x) = x^3 - 5x^2 - 4x + 20$

A) $x = 5, x = -2, x = 2$

C) $x = -5, x = -2, x = 2$

$x^2(x-5) - 4(x-5)$

$(x^2-4)(x-5)$

$x = 2, -2, 5$

B) $x = -2, x = 2$

D) $x = 5, x = 4$

13) A

Find the zeros for the polynomial function and give the multiplicity for each zero. State whether the graph crosses the x-axis or touches the x-axis and turns around, at each zero.

14) $f(x) = 5(x+1)(x+4)^3$

A) -1, multiplicity 1, crosses x-axis; -4, multiplicity 3, crosses x-axis

B) -1, multiplicity 1, crosses x-axis; -4, multiplicity 3, touches x-axis and turns around

C) 1, multiplicity 1, touches x-axis; 4, multiplicity 3, touches x-axis and turns around

D) 1, multiplicity 1, crosses x-axis; 4, multiplicity 3, crosses x-axis

$x = -1, -4$

14) A

15) $f(x) = 3(x^2 + 1)(x - 2)^2$

A) 2, multiplicity 2, crosses the x-axis

B) -1, multiplicity 1, crosses the x-axis; 2, multiplicity 2, touches the x-axis and turns around.

C) 2, multiplicity 2, touches the x-axis and turns around

D) -1, multiplicity 1, crosses the x-axis; 2, multiplicity 2, crosses the x-axis

$x = 2$

15) C

Use the Intermediate Value Theorem to determine whether the polynomial function has a real zero between the given integers.

16) $f(x) = -4x^4 - 2x^2 + 4$; between -1 and 0

A) $f(-1) = 2$ and $f(0) = -4$; yes

C) $f(-1) = -2$ and $f(0) = -4$; no

$f(-1) = -4(-1)^4 - 2(-1)^2 + 4 = -4 - 2 + 4 = -2$

B) $f(-1) = 2$ and $f(0) = 5$; no

D) $f(-1) = -2$ and $f(0) = 4$; yes

$f(0) = 4$

16) D

Determine the maximum possible number of turning points for the graph of the function.

17) $f(x) = 9x^8 - 4x^7 - 5x - 18$

A) 9

B) 8

C) 0

D) 7

turns = $n - 1$

↑
degree

17) D

Solve the problem.

18) Solve the equation $3x^3 - 32x^2 + 73x + 28 = 0$ given that 4 is a zero of $f(x) = 3x^3 - 32x^2 + 73x + 28$.

A) $\left\{4, 1, -\frac{7}{3}\right\}$

B) $\left\{4, 7, -\frac{1}{3}\right\}$

C) $\left\{4, -7, \frac{1}{3}\right\}$

D) $\left\{4, -1, \frac{7}{3}\right\}$

$$\begin{array}{r|rrrr} 4 & 3 & -32 & 73 & 28 \\ & & 12 & -80 & -28 \\ \hline & 3 & -20 & -7 & 0 \end{array}$$

$3x^2 - 20x - 7 = 0$

$(3x + 1)(x - 7) = 0$

$x = -\frac{1}{3}, 7$

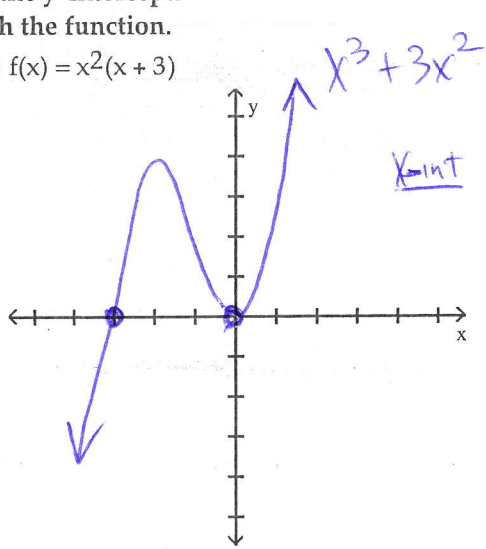
18) B

SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

Complete the following:

- Use the Leading Coefficient Test to determine the graph's end behavior.
- Find the x-intercepts. State whether the graph crosses the x-axis or touches the x-axis and turns around at each intercept.
- Find the y-intercept.
- Graph the function.

19) $f(x) = x^2(x + 3)$



x-int $x^2(x+3) = 0$
 $x = 0, -3$

y-int $f(0) = 0^2(0+3) = 0$

- 19) ←
 a) falls left, rises right
 b) (0,0) touches
(-3,0) crosses
 c) (0,0)
 d) see left

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Divide using long division.

20) $\frac{x^4 + 3x^3 + 6x^2 + 5x + 9}{x^2 + 2x + 3}$

A) $x^2 + x + 1 + \frac{6}{x^2 + 2x + 3}$

C) $x^2 + x + 1$

$x^2 + 2x + 3 \overline{) x^4 + 3x^3 + 6x^2 + 5x + 9}$
 $(-) x^4 + 2x^3 + 3x^2$

$x^3 + 3x^2 + 5x$
 $(-) x^3 + 2x^2 + 3x$

$x^2 + 4x + 17 + \frac{49x + 48}{x^2 + 2x + 3}$

20) A

21) $\frac{8m^4 + 12m^3 - 2m}{2m^2 + m}$

A) $4m^2 + 8m + 4 + \frac{2m}{2m^2 + m}$

C) $4m^2 + 4m - \frac{6m}{2m^2 + m}$

$2m^2 + m \overline{) 8m^4 + 12m^3 + 0m^2 - 2m}$
 $(-) 8m^4 + 4m^3$

$8m^3 + 0m^2$
 $(-) 8m^3 + 4m^2$

$-4m^2 - 2m$
 $(-) -4m^2 - 2m$
0

21) D

Divide using synthetic division.

22) $\frac{-4x^3 - 16x^2 + 18x - 10}{x + 5}$

A) $4x^2 - 5x - 2$

C) $-\frac{4}{5}x^2 - \frac{16}{5}x + \frac{18}{5}$

$-5 \overline{) -4 \ -16 \ 18 \ -10}$
 $\underline{20 \ -20 \ 10}$
 $-4 \ 4 \ -2 \ 0$

B) $-4x^2 + 4x - 2$

D) $-4x^2 - \frac{16}{5} - 2$

22) B

Use synthetic division and the Remainder Theorem to find the indicated function value.

23) $f(x) = 3x^3 - 5x^2 - 4x + 2; f(-2)$

A) -50

B) -14

C) -4

D) -34

$$\begin{array}{r|rrrr} -2 & 3 & -5 & -4 & 2 \\ & & -6 & 22 & -36 \\ \hline & 3 & -11 & 18 & -34 \end{array}$$

23) D

Find an nth degree polynomial function with real coefficients satisfying the given conditions.

24) $n = 3$; -2 and $-3 + 2i$ are zeros; leading coefficient is 1

A) $f(x) = x^3 - 4x^2 + 25x + 26$

B) $f(x) = x^3 + 5x^2 + 25x - 14$

C) $f(x) = x^3 + 8x^2 + 15x + 26$

D) $f(x) = x^3 + 8x^2 + 25x + 26$

$$1(x+2)(x+3-2i)(x+3+2i) = (x+2)(x^2+3x+2xi+3x+9+6i-2xi-6i-4(-2))$$

24) D

Use Descartes's Rule of Signs to determine the possible number of positive and negative real zeros for the given function.

25) $f(x) = x^7 + x^6 + x^2 + x + 2$

A) 0 positive zeros, 0 negative zeros

B) 0 positive zeros, 1 negative zero

C) 0 positive zeros, 3 or 1 negative zeros

D) 0 positive zeros, 2 or 0 negative zeros

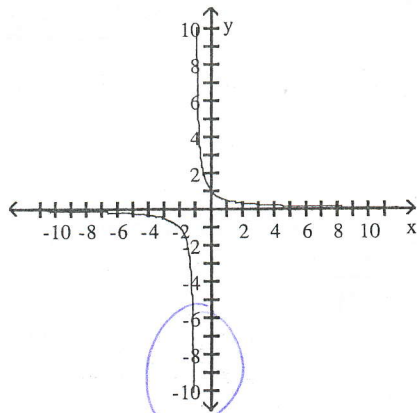
$$-x^7 + x^6 + x^2 - x + 2$$

pos: 0
neg: 3 or 1

25) C

Use the graph of the rational function shown to complete the statement.

26)



As $x \rightarrow -1^-$, $f(x) \rightarrow ?$

A) $+\infty$

B) $-\infty$

C) 1

D) 0

26) B

Find the vertical asymptotes, if any, of the graph of the rational function.

27) $g(x) = \frac{x}{x^2 - 25} = 0 \quad (x-5)(x+5) = 0$

A) $x = 5$

B) $x = 5, x = -5$

C) $x = 5, x = -5, x = 0$

D) no vertical asymptote

27) B

Find the horizontal asymptote, if any, of the graph of the rational function.

28) $g(x) = \frac{4x^2 - 2x - 8}{6x^2 - 7x + 5}$

$$y = \frac{4}{6} = \frac{2}{3}$$

A) $y = \frac{2}{7}$

B) $y = 0$

C) $y = \frac{2}{3}$

D) no horizontal asymptote

28) C

Find the slant asymptote, if any, of the graph of the rational function.

29) $f(x) = \frac{x^2 + 9x - 3}{x - 5}$

- A) $y = x$
- C) $y = x + 14$**

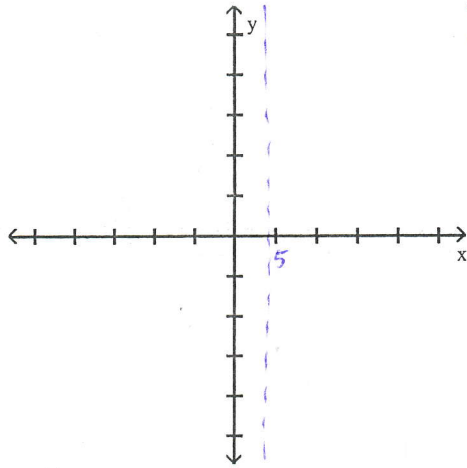
$$\begin{array}{r} x+14 \\ x-5 \overline{) x^2+9x-3} \\ \underline{x^2-5x} \\ 14x-3 \end{array}$$

- B) $y = x + 9$
- D) no slant asymptote

29) C

Graph the function.

30) $f(x) = \frac{x^2 + 7x - 7}{x - 3}$

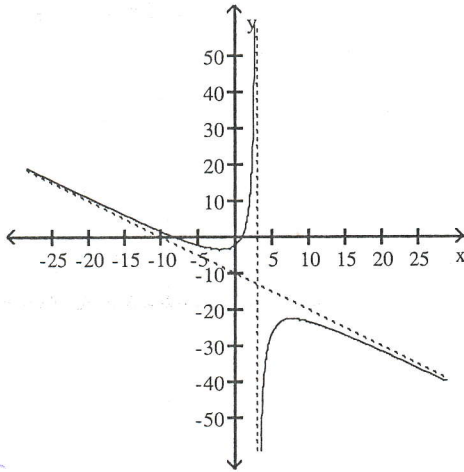


$$\begin{array}{l} x-3=0 \\ x=3 \end{array}$$

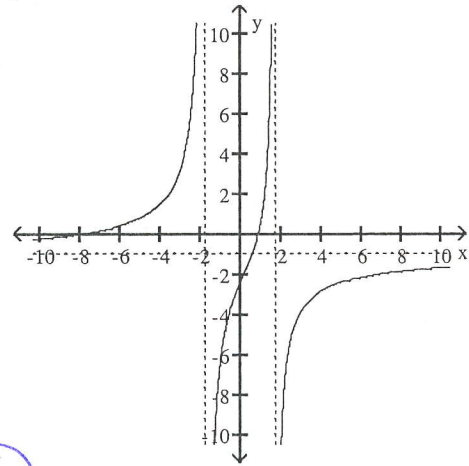
$$\begin{array}{r} x+10 \\ x-3 \overline{) x^2+7x-7} \\ \underline{x^2-3x} \\ 10x-7 \end{array}$$

30) D

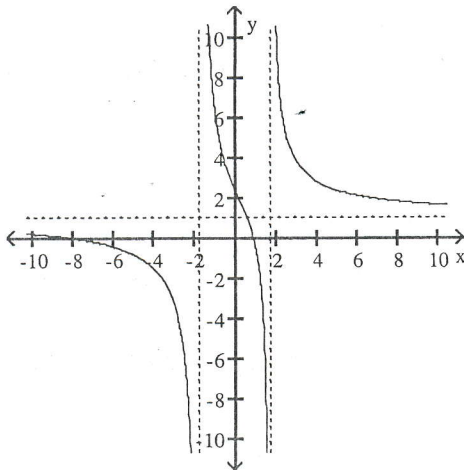
A)



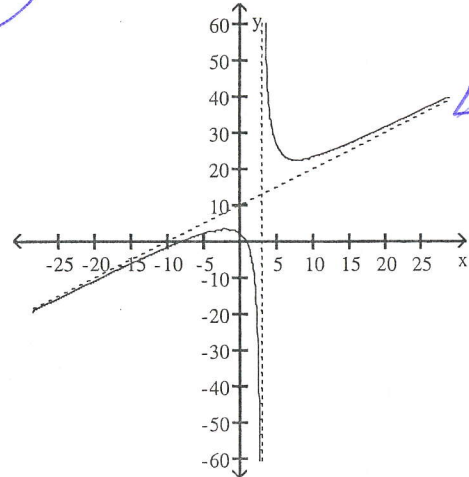
~~B)~~



~~C)~~



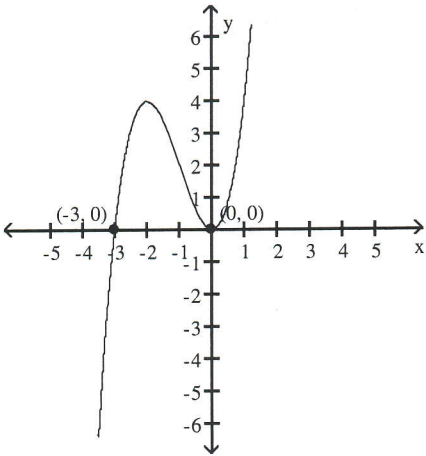
D)



Pre-Calculus
Practice Test

- 1) D
- 2) A
- 3) D
- 4) A
- 5) A
- 6) A
- 7) C
- 8) D
- 9) D
- 10) C
- 11) C
- 12) C
- 13) A
- 14) A
- 15) C
- 16) D
- 17) D
- 18) B

- 19) (a) falls to the left and rises to the right
(b) x-intercepts: $(0, 0)$, touches x-axis and turns; $(-3, 0)$, crosses x-axis
(c) y-intercept: $(0, 0)$
(d)



- 20) A
- 21) D
- 22) B
- 23) D
- 24) D
- 25) C
- 26) B
- 27) B
- 28) C
- 29) C
- 30) D