

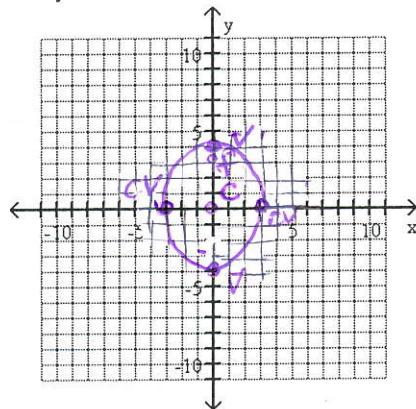
TRIG
Chapter 9 Practice Test

Name Kley

SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

Graph the ellipse and label all of the important pieces.

1) $16x^2 + 9y^2 = 144$



$$\frac{16x^2}{144} + \frac{9y^2}{144} = 1$$

$$\frac{x^2}{9} + \frac{y^2}{16} = 1$$

$$a^2 - b^2 = c^2$$

$$16 - 9 = c^2$$

$$7 = c^2$$

$$\sqrt{7} = c$$

1) ←

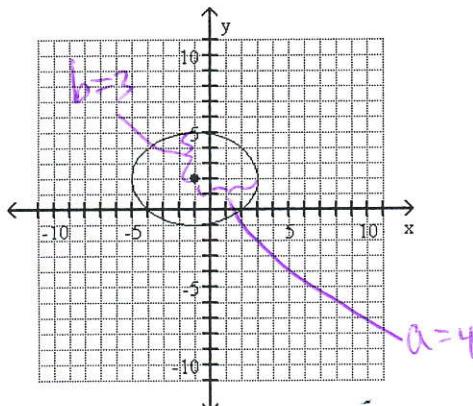
Convert the equation to the standard form for a hyperbola by completing the square on x and y.

2) $4x^2 - 16y^2 + 16x - 64y - 112 = 0$

$$\begin{aligned} 4x^2 + 16x & - 16y^2 - 64y - 112 = 0 \\ 4(x^2 + 4x + 4) - 16(y^2 + 4y + 4) & - 112 - 16 + 64 = 0 \\ 4(x+2)^2 - 16(y+2)^2 & = 64 \end{aligned}$$

Find the standard form of the equation of the ellipse and give the location of its foci.

3)



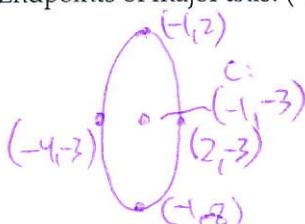
Center at $(-1, 2)$

$$\frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2} = 1$$

$$\frac{(x+1)^2}{4^2} + \frac{(y-2)^2}{3^2} = 1$$

Find the standard form of the equation of the ellipse satisfying the given conditions.

4) Endpoints of major axis: $(-1, -8)$ and $(-1, 2)$; endpoints of minor axis: $(-4, -3)$ and $(2, -3)$;



$$\frac{(x-h)^2}{b^2} + \frac{(y-k)^2}{a^2} = 1$$

$$\frac{(x+1)^2}{3^2} + \frac{(y+3)^2}{5^2} = 1$$

4) ←

5) Major axis horizontal with length 18; length of minor axis = 10; center (0, 0)

$$\frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2} = 1 \quad \frac{x^2}{9^2} + \frac{y^2}{5^2} = 1$$

$$5) \frac{x^2}{81} + \frac{y^2}{25} = 1$$

6) Foci: (-6, 0), (6, 0); x-intercepts: -8 and 8

$$\frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2} = 1 \quad \frac{x^2}{8^2} + \frac{y^2}{b^2} = 1$$

$$c=6 \quad a^2 - b^2 = c^2 \rightarrow 8^2 - b^2 = 6^2$$

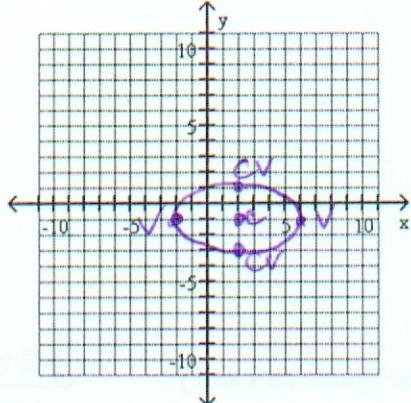
$$-b^2 = 36 - 64$$

$$b^2 = 28$$

$$6) \frac{x^2}{64} + \frac{y^2}{28} = 1$$

Graph the ellipse. Label all of the important pieces.

$$7) \frac{(x-2)^2}{16} + \frac{(y+1)^2}{4} = 1 \quad C: (2, -1)$$



$$7) \underline{\hspace{2cm}} \leftarrow$$

Find the standard form of the equation of the hyperbola satisfying the given conditions.

8) Endpoints of transverse axis: (0, -8), (0, 8); asymptote: $y = \frac{4}{9}x$

$$\frac{(y-h)^2}{a^2} - \frac{(x-k)^2}{b^2} = 1 \quad \frac{y^2}{8^2} - \frac{x^2}{b^2} = 1$$

$$\frac{4}{9} = \frac{8}{b} \\ b=18$$

$$8) \frac{y^2}{64} - \frac{x^2}{324} = 1$$

9) Foci: (-10, 0), (10, 0); vertices: (-6, 0), (6, 0) $C: (0, 0)$

$$\frac{(x-h)^2}{a^2} - \frac{(y-k)^2}{b^2} = 1 \quad a^2 + b^2 = c^2$$

$$6^2 + b^2 = 10^2$$

$$b^2 = 100 - 36 \quad b^2 = 64$$

$$9) \frac{x^2}{36} - \frac{y^2}{64} = 1$$

10) Center: (4, 6); Focus: (1, 6); Vertex: (3, 6)

$$\frac{(x-h)^2}{a^2} - \frac{(y-k)^2}{b^2} = 1 \quad a^2 + b^2 = c^2$$

$$1^2 + b^2 = 3^2$$

$$b^2 = 9 - 1 \quad b^2 = 8$$

$$10) \frac{(x-4)^2}{1} - \frac{(y-6)^2}{8} = 1$$

Convert the equation to the standard form for a hyperbola by completing the square on x and y.

$$11) y^2 - 4x^2 - 4y + 8x - 4 = 0$$

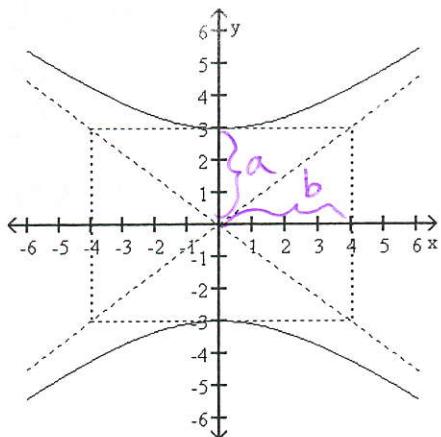
$$\begin{aligned} y^2 - 4y &\quad -4x^2 + 8x \\ y^2 - 4y + 4 &\quad -4(x^2 - 2x + 1) \\ (y-2)^2 - 4 &\quad -4(x-1)^2 \end{aligned}$$

$$\begin{array}{r} -4 \\ +4 \\ \hline = 4 \end{array}$$

$$11) \frac{(y-2)^2}{4} - \frac{(x-1)^2}{1} = 1$$

Find the standard form of the equation of the hyperbola.

12)



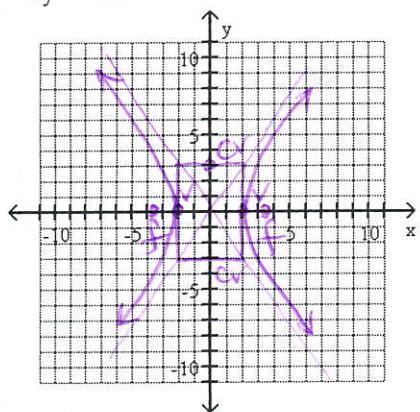
$$12) \frac{y^2}{9} - \frac{x^2}{16} = 1$$

$$\frac{(y-k)^2}{a^2} - \frac{(x-h)^2}{b^2} = 1$$

$$\frac{y^2}{3^2} - \frac{x^2}{4^2} = 1$$

Find center, vertices, covertices, foci and asymptotes and graph the hyperbola.

$$13) 9x^2 - 4y^2 = 36$$



$$\frac{x^2}{4} - \frac{y^2}{9} = 1$$

$$\begin{aligned} a^2 + b^2 &= c^2 \\ 4 + 9 &= c^2 \\ 13 &= c^2 \end{aligned}$$

$$13) C: (0, 0)$$

$$V: (\pm 2, 0)$$

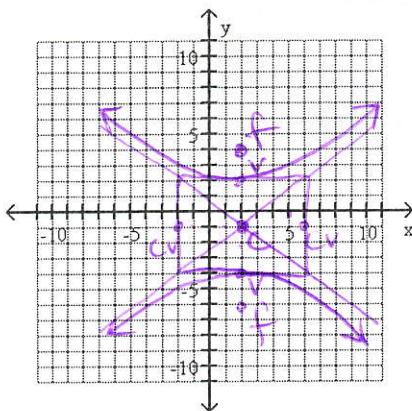
$$CV: (0, \pm 3)$$

$$F: (\pm \sqrt{13}, 0)$$

$$\text{Asymp: } y = \pm \frac{3}{2}x$$

Find the center, vertices, covertices, foci and asymptotes to graph the hyperbola.

$$14) \frac{(y+1)^2}{9} - \frac{(x-2)^2}{16} = 1$$



C:

$$a^2 + b^2 = c^2$$

$$9 + 16 = c^2$$

$$5 = c$$

$$14) \begin{array}{l} C: (2, -1) \\ V: (2, 2), (2, -4) \\ CV: (6, -1), (-2, -1) \\ F: (2, 4), (2, -6) \end{array}$$

Convert the equation to the standard form for a parabola by completing the square on x or y as appropriate.

$$15) x^2 - 4x + 3y - 5 = 0$$

$$\begin{aligned} x^2 - 4x + 4 & - 4 + 3y - 5 = 0 \\ (x-2)^2 & = -3y + 9 \end{aligned}$$

$$15) \underline{(x-2)^2 = -3(y-3)}$$

Find the focus and directrix of the parabola with the given equation.

$$16) x^2 = 40y$$

$$\begin{aligned} x^2 &= 4py \\ p &= 10 \end{aligned}$$

$$16) \begin{array}{l} f: (0, 10) \\ d: y = -10 \end{array}$$

Find the vertex, focus, and directrix of the parabola with the given equation.

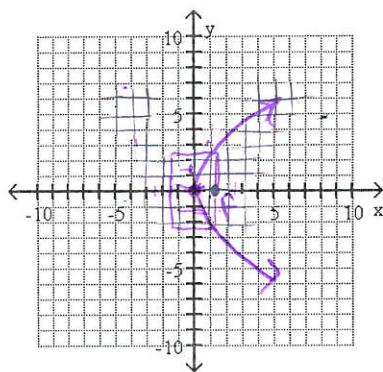
$$17) (x-2)^2 = 4(y+1)$$

$$\begin{aligned} V: (2, -1) \\ 4p &= 1 \\ p &= \frac{1}{4} \end{aligned}$$

$$17) \begin{array}{l} V: (2, -1) \\ F: (2, 0) \\ d: y = -2 \end{array}$$

Graph the parabola.

$$18) y^2 = 5x$$

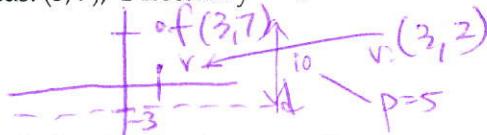


$$\begin{aligned} y^2 &= 4px \\ 4p &= 5 \\ p &= \frac{5}{4} \end{aligned}$$

$$18) \underline{\hspace{1cm}}$$

Find the standard form of the equation of the parabola using the information given.

- 19) Focus: (3, 7); Directrix: $y = -3$



$$(x-3)^2 = 4(5)(y)$$

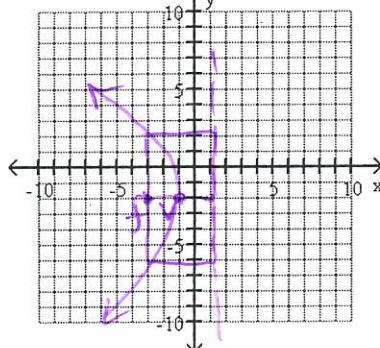
19) $(x-3)^2 = 20(y-2)$

Graph the parabola with the given equation.

- 20) $(y+2)^2 = -8(x+1)$

$$4p \quad p=-2$$

$$\leftarrow \quad V: (-1, -2)$$



20) \leftarrow

Identify the equation without completing the square.

- 21) $2x^2 - 2x + y + 4 = 0$

21) $2x^2 - 2x + y + 4 = 0$

21) parabola

- 22) $2x^2 + 4y^2 + 8x + 4y = 0$

$A=C>0$

22) ellipse

- 23) $4x^2 - 4y^2 + 5x + 4y + 3 = 0$

$A-C<0$

23) hyperbola

- 24) $5x^2 - 6y^2 + 2x - 3y - 5 = 0$

$A-C<0$

24) hyperbola

- 25) $2y^2 - 3x + 2y = 0$

25) $2y^2 - 3x + 2y = 0$

25) parabola