

**Topic 5** enVision™ STEM Project

Introduction to Nonlinear Functions

BLM 1

Model an Insect Population, Part 1

The function below models a cicada population:

$$f(x) = k \cdot f(x - 1) \cdot [1 - f(x - 1)], \text{ where } f(0) = 0.1$$

$$\text{and } f(1) = k(0.1) \cdot (1 - 0.1)$$

The constant k , between 0 and 4, is the growth parameter that controls how quickly the population grows.

For each value of k below, find the point at which the population is stable. Explain how you know the population is stable.

$k = 2$	$k = 1$	$k = 1.5$

Name _____



Topic 5 enVision™ STEM Project

Introduction to Nonlinear Functions

BLM 2

Model an Insect Population, Part 2

The function below models a cicada population:

$$f(x) = k \cdot f(x - 1) \cdot [1 - f(x - 1)], \text{ where } f(0) = 0.1$$

$$\text{and } f(1) = k(0.1) \cdot (1 - 0.1)$$

What happens to the population for each value of k below? Explain your findings.

$k = 0.5$	$k = 3$	$k = 4$

Name _____



Topic 5 enVision™ STEM Project

Introduction to Nonlinear Functions

BLM 3

Model an Insect Population, Part 3

The function below models a cicada population:

$$f(x) = k \cdot f(x - 1) \cdot [1 - f(x - 1)], \text{ where } f(0) = 0.099$$

$$\text{and } f(1) = k(0.099) \cdot (1 - 0.099)$$

What happens to the population for each value of k below? Explain your findings.

$k = 2$	$k = 1$	$k = 4$



Topic 5 enVision™ STEM Project

Introduction to Nonlinear Functions

BLM 4

Analyze an Insect Population

What would be the best value of k for an insect population, and why?

What would happen if human interaction caused changes to the value of k (increases or decreases)?

Extension Why do you think k is limited to between 0 and 4?

Extension If the previous population is p , what do the terms p and $(1 - p)$ represent for determining the next population?

Extension Try to find values of $f(0)$ and k that reproduce the 17-year cicada's behavior.