

TOPIC
8

Topic Review

? TOPIC ESSENTIAL QUESTION

- How can you use sketches and equations of quadratic functions to model situations and make predictions?

Vocabulary Review

Choose the correct term to complete each sentence.

- The graph of a quadratic function is a(n) parabola.
- The function $f(x) = x^2$ is called the quadratic parent function.
- To model the height of an object launched into the air t seconds after it is launched, you can use the vertical motion model.
- The standard form of a quadratic function is $f(x) = ax^2 + bx + c$.
- A(n) quadratic regression is a method used to find a quadratic function that best fits a data set.

- parabola
- quadratic parent function
- quadratic regression
- standard form of a quadratic function
- vertex form of a quadratic function
- vertical motion model

Concepts & Skills Review

LESSON 8-1 Key Features of Quadratic Functions

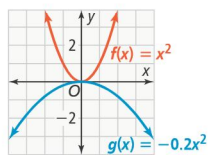
Quick Review

The graph of $f(x) = ax^2$ is a parabola with vertex $(0, 0)$ and axis of symmetry $x = 0$. When $a > 0$, pos. the parabola opens upward and the function has a minimum at the vertex. When $a < 0$, neg. the parabola opens downward and the function has a maximum at the vertex.

Example

Compare the graph of $g(x) = -0.2x^2$ with the graph of $f(x) = x^2$.

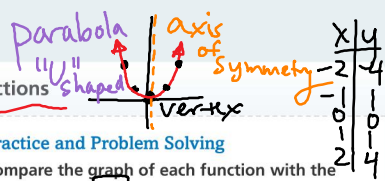
The graph of g opens downward and is wider than the graph of f . For both graphs, the axis of symmetry is $x = 0$ and the vertex is $(0, 0)$.



Practice and Problem Solving

Compare the graph of each function with the graph of $f(x) = x^2$.

- $g(x) = 1.5x^2$ (Vert. stretch) and $h(x) = -9x^2$ (Vert. stretch & reflected)
- Communicate Precisely** Explain how you can tell whether a function of the form $f(x) = ax^2$ has a minimum or a maximum value and what that value is.
- Model With Mathematics** Artificial turf costs \$15/sq ft to install, and sod costs \$0.15/sq ft to install. Write a quadratic function that represents the cost of installing artificial turf on a square plot with a side length of x feet, and a second quadratic function that represents the cost of installing sod on the same plot. How do the graphs of the two functions differ?



TOPIC 8 REVIEW

LESSON 8-2 Quadratic Functions in Vertex Form

Quick Review

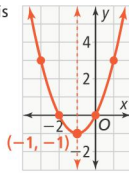
The **vertex form** of a quadratic function is $f(x) = a(x - h)^2 + k$. The **vertex** of the graph is at (h, k) and the axis of symmetry is $x = h$.

Example

Graph the function $f(x) = (x + 1)^2 - 1$.

The vertex is $(-1, -1)$ and the axis of symmetry is $x = -1$.

Use the points $(0, 0)$ and $(1, 3)$ to find two other points. Reflect each point across the axis of symmetry.



$a(x-h)^2 + k$
 • opens downward ($a < 0$)
 • same vertex: $(3, 2)$

Practice and Problem Solving

11. Look for Relationships Graph the functions below. How are the graphs alike? How are the graphs different from each other?

$f(x) = (-5)(x - 3)^2 + 2$
 $g(x) = (-2)(x - 3)^2 + 2$

• $f(x)$ is stretched more... (narrower)

Identify the vertex and axis of symmetry of the graph of each function.

12. $g(x) = (x + 8)^2 + 1$ **13.** $h(x) = (x - 5)^2 - 2$

12) $V: (-8, 1)$
 AOS: $x = -8$

13) $V: (5, -2)$
 AOS: $x = 5$

14. An astronaut on the moon throws a moon rock into the air. The rock's height, in meters, above the moon's surface x seconds after it is thrown can be determined by the function $h(x) = -1.6(x - 2.5)^2 + 15$. What is the maximum height of the rock above the moon's surface? How many seconds after being thrown does the rock reach this height?

LESSON 8-3 Quadratic Functions in Standard Form

Quick Review

The **standard form** of a quadratic function is $f(x) = ax^2 + bx + c$, where $a \neq 0$. The **y-intercept** is $(0, c)$ and the axis of symmetry, which is also the x -coordinate of the vertex, is $x = -\frac{b}{2a}$.

Example

Graph the function $f(x) = 3x^2 - 6x + 2$.

The y -intercept is 2.

Find the axis of symmetry.

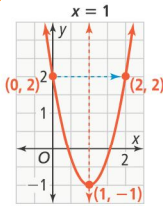
$x = -\frac{b}{2a} = -\frac{-6}{2(3)} = 1$

Find the y -coordinate of the vertex.

$f(1) = 3(1)^2 - 6(1) + 2 = -1$

Plot the vertex $(1, -1)$ and identify the axis of symmetry.

Plot the y -intercept $(0, 2)$. Reflect that point across the axis of symmetry.



Practice and Problem Solving

Identify the y -intercept, axis of symmetry, and vertex of the graph of each function.

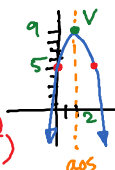
15. $g(x) = -x^2 + 4x + 5$ **16.** $h(x) = -3x^2 + 7x + 1$

17. When given a function in standard form, how can you determine if the parabola has a minimum or maximum value?

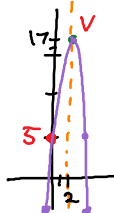
18. Graph the function $f(x) = -3x^2 + 12x + 5$.

19. Reason A ball is tossed into the air. The function $f(x) = -16x^2 + 4x + 5$ represents the height in feet of the ball x seconds after it is thrown. At what height was the ball tossed into the air?

$ax^2 + bx + c$
15) y -int: 5
 AOS: $x = -\frac{b}{2a} = -\frac{4}{2(-1)} = 2$
 Vertex: $(2, 9)$



18) y -int: 5
 AOS: $x = -\frac{b}{2a} = -\frac{12}{2(-3)} = 2$
 Vertex: $(2, 17)$



$f(2) = -3(2)^2 + 12(2) + 5$
 $= -3 \cdot 4 + 24 + 5$
 $= -12 + 24 + 5$
 $= 12 + 5 = 17$

LESSON 8-4 Modeling With Quadratic Functions

Quick Review

Quadratic functions can model situations. For example, the vertical motion model is a quadratic function.

Example

Alberto launches an emergency flare at an initial velocity of 64 ft/s from an initial height of 6 ft. The flare must reach a height of 100 ft to be seen by a rescue team. Is Alberto's launch successful?

Substitute 64 for v_0 and 6 for h_0 in the vertical motion model.

$$h(t) = -16t^2 + 64t + 6$$

Find the vertex $(t, h(t))$.

$$t = -\frac{b}{2a} = -\frac{64}{2(-16)} = 2$$

$$h(2) = -16(2)^2 + 64(2) + 6 = 70$$

The vertex is $(2, 70)$.


The flare will reach a maximum height of 70 ft, so Alberto's launch is not successful.


Practice and Problem Solving

Write a function h to model the vertical motion for each situation, given $h(t) = -16t^2 + v_0t + h_0$. Find the maximum height.

- 20. initial velocity: 54 ft/s
initial height: 7 ft
- 21. initial velocity: 18 ft/s
initial height: 9 ft

Write a quadratic function to represent the area of each rectangle. Graph the function. Interpret the vertex and intercepts. Identify a reasonable domain and range.

22.  $2x - 1$

23.  $x + 1$

- 24. **Make Sense and Persevere** Given a vertical motion model, how can you identify the amount of time an object is in the air before it reaches the ground?

LESSON 8-5 Linear, Exponential, and Quadratic Models

Quick Review

To determine which function best models a data set, analyze the differences and ratios between consecutive y -values when the differences in consecutive x -values are constant.

Example

Determine whether the function below is linear, quadratic, or exponential.

x	y	1st Diff.	2nd Diff.	Ratios
0	1			
1	3	2		3
2	9	6	4	3
3	27	18	12	3

Since the ratio between the y -values is constant, the function is exponential.

Practice and Problem Solving

- 25. **Make Sense and Persevere** What is the first step in determining whether a table shows a linear, quadratic, or exponential function?

Determine whether the data in the tables represent a linear, quadratic, or exponential function.

26.

x	0	1	2	3	4
y	3	7	19	39	67

27.

x	-2	0	2	4	6
y	-20	-6	8	22	36