



**UNDERSTAND**

20. **Use Structure** For  $\sqrt{x^n}$ , consider rewriting this expression without a perfect square factor in the radicand for even and odd values of  $n$ , where  $n$  is a positive integer.
- What is the expression when  $n$  is even?
  - What is the expression when  $n$  is odd?
21. **Error Analysis** Describe and correct the error a student made in multiplying  $2\sqrt{7x^2}$  by  $2\sqrt{14x^3}$ .

$$\begin{aligned}
 & 2\sqrt{7x^2} \cdot 2\sqrt{14x^3} \\
 &= 2 \cdot 2\sqrt{7x^2 \cdot 14x^3} \\
 &= 4\sqrt{7 \cdot 2 \cdot 7 \cdot x \cdot x \cdot x \cdot x \cdot x} \\
 &= 8 \cdot 7\sqrt{x^2 \cdot x^2 \cdot x} \\
 &= 56x^2\sqrt{x}
 \end{aligned}$$



22. **Use Structure** Find  $\sqrt{591x^{15}y^3} \cdot \sqrt{591x^{15}y^3}$  without calculating or simplifying.
23. **Communicate Precisely** Why do the multiplication properties of exponents apply to radicals? Explain.
24. **Make Sense and Persevere** How many perfect squares are under each radical?

Radical	Perfect squares
$\sqrt{8}$	
$\sqrt{18}$	
$\sqrt{32x^6}$	
$\sqrt{50x}$	
$\sqrt{72}$	

25. **Higher Order Thinking** Can you use the Product Property of Square Roots to find equivalent expressions for each radical? Explain.
- $\sqrt[3]{24x^8}$
  - $\sqrt[4]{3^9x^{13}}$

**PRACTICE**

Compare each pair of radical expressions.

SEE EXAMPLE 1

- $6\sqrt{3}$  and  $\sqrt{108}$
- $2\sqrt{21}$  and  $4\sqrt{5}$
- $40\sqrt{42}$  and  $42\sqrt{40}$
- $\frac{1}{2}\sqrt{120}$  and  $\sqrt{30}$
- $\sqrt{68}$  and  $2\sqrt{18}$
- $\sqrt{96}$  and  $3\sqrt{15}$

Write each expression so the radicand has no perfect squares other than 1. SEE EXAMPLES 2 AND 3

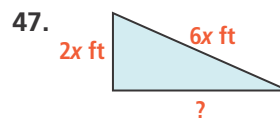
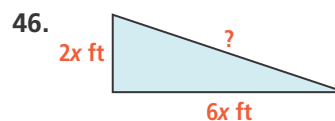
- $\sqrt{210}$
- $\sqrt{250}$
- $\sqrt{108}$
- $2\sqrt{21}$
- $\sqrt{98x^8}$
- $\sqrt{200x^3}$
- $\sqrt{32x^4y^3}$
- $4x\sqrt{\frac{1}{4}x^6}$

Write each expression so the radicand has no perfect squares other than 1. SEE EXAMPLE 4

- $\sqrt{12x} \cdot \sqrt{3x}$
- $\sqrt{2x^9} \cdot \sqrt{26x^6}$
- $\sqrt{27m} \cdot \sqrt{6m^{20}}$
- $\sqrt{2x^3} \cdot \sqrt{25x^2y}$
- $\sqrt{9x^9} \cdot \sqrt{18x^3}$
- $\sqrt{32x} \cdot \sqrt{72x^{18}}$

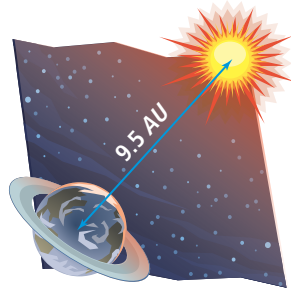
Write an expression in simplest form for the missing side length. Then find the side lengths of each triangle to the nearest tenth when  $x = 15$ .

SEE EXAMPLE 5



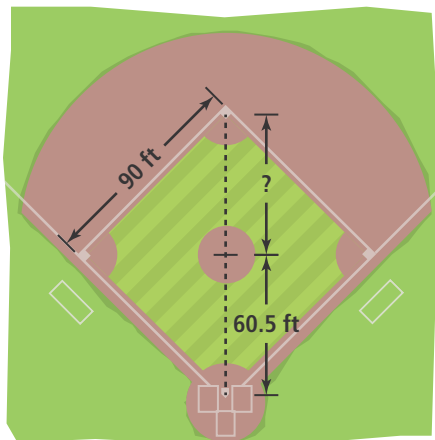
**APPLY**

48. **Use Structure** The time it takes a planet to revolve around the sun in Earth years can be modeled by  $t = \sqrt{d^3}$ , where  $d$  is the average distance from the sun in astronomical units (AU).



- Write an equivalent equation for the function.
- How long does it take Saturn, pictured above, to orbit the sun? Show that both expressions give the same value.

49. **Model With Mathematics** A baseball “diamond” is a square that measures 90 ft on each side.



- Write an expression for the distance from 2<sup>nd</sup> base to home plate in feet. What is this distance to the nearest tenth?
- The pitcher standing on the pitcher’s mound is about to throw to home plate but turns around and throws to 2<sup>nd</sup> base. How much farther is the throw? Explain.

50. **Model With Mathematics** A framed television has a ratio of width to height of about 1.732 : 1.

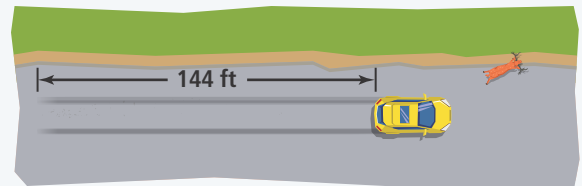
- For a television with a height of  $h$  inches, what is an equivalent expression for the length of the diagonal? Justify your answer.
- Write an expression for the perimeter.

**ASSESSMENT PRACTICE**

51. Copy and complete the table. Find the product of each row and column without a perfect square factor in the radicand and enter it in the appropriate cell.

	$\sqrt{48}$	$5x\sqrt{6x^3}$
$\sqrt{12}$	■	■
$2x\sqrt{6x}$	■	■
$4x^2\sqrt{2x^5}$	■	■

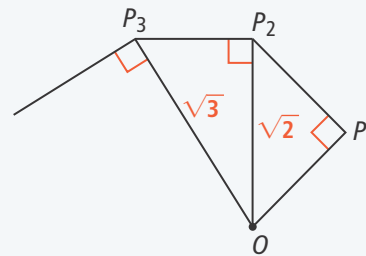
52. **SAT/ACT** A car skidded  $s$  ft when traveling on a damp paved road. The expression  $r = \sqrt{18s}$  is an estimate of the car’s rate of speed in ft/s.



Which expression represents the speed of the car in feet per second?

- $24\sqrt{6}$
- $12\sqrt{6}$
- $36\sqrt{2}$
- $24\sqrt{3}$
- $48\sqrt{2}$

53. **Performance Task** Copy the figure. Center it on a large piece of paper so you can expand it.



**Part A** Use the pattern to complete the triangle on the left. Label the side lengths.

**Part B** Continue using the pattern to add triangles while labeling side lengths.

**Part C** Are equivalent expressions of the square roots appropriate? Explain your reasoning.