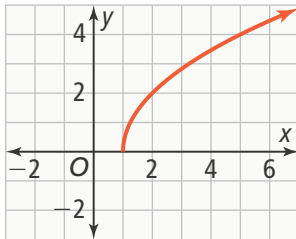




**UNDERSTAND**

- Communicate Precisely** What is the domain and range of the radical function  $h(x) = \sqrt{x+a} + b$ ? Is the function increasing or decreasing? Explain.
- Model with Mathematics** The graph of a cube root function has a horizontal translation that is three times the vertical translation. The vertical translation is negative.
  - Write a function,  $g$ , that has these attributes.
  - Graph your function and the parent function,  $f$ , to verify it is correct.
- Error Analysis** Helena is trying to write a radical function that is represented by the graph below. Describe and correct the error Helena made in writing the radical function.



$f(x) = \sqrt{x-1}$  **X**

- Higher Order Thinking** Rewrite the radical function  $g(x) = \sqrt[3]{8x+64} - 3$  to identify the transformations from the parent graph of  $f(x) = \sqrt[3]{x}$ . Explain how you rewrote the radical function.
- Reason** The parent function  $f(x) = \sqrt{x}$  and a transformation of the parent function,  $g(x)$ , are reflections of each other over the  $x$ -axis. Write the function  $g(x)$ .
- Mathematical Connections** How do the transformations of a radical function compare to the transformations of an absolute value function?

**PRACTICE**

Graph the following functions. State the domain and range. Is the function increasing or decreasing? SEE EXAMPLE 1

- $f(x) = \sqrt{x} + 2$
- $f(x) = \sqrt[3]{x} - 4$
- $f(x) = \sqrt[3]{x-8}$
- $f(x) = \sqrt{x+6}$

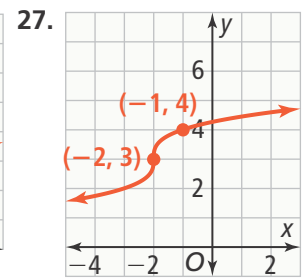
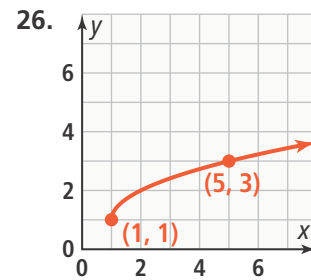
21. Graph  $f(x) = \sqrt[3]{x}$  and  $g(x) = 3\sqrt[3]{x+9} - 8$ . What transformations of the graph of  $f$  produce the graph of  $g$ ? What effect do the transformations have on the domain and range of  $g$ ?

SEE EXAMPLE 2

Rewrite the following radical functions to identify their transformations from the parent graph  $f(x) = \sqrt{x}$ . SEE EXAMPLE 3

- $f(x) = \sqrt{16x}$
- $f(x) = \sqrt{25x+75}$
- $f(x) = \sqrt{9x-45}$
- $f(x) = \sqrt{4x-24} - 6$

What radical function is represented in each graph? SEE EXAMPLE 4



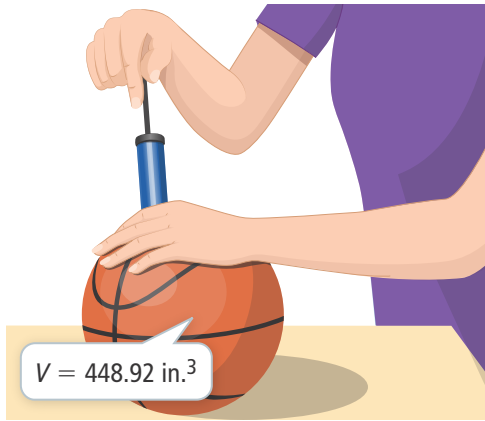
28. The hull speed,  $y$ , measured in knots, of a sailboat can be estimated by the function  $y = 1.34\sqrt{x}$ , where  $x$  is the waterline length of the sailboat, in feet. Luis works at a sailboat rental business with boats that have a waterline length between 25 ft and 64 ft. SEE EXAMPLE 5

- Graph the relationship between the hull speed of a sailboat and its waterline length.
- What are the minimum and maximum hull speeds of the sailboats at the rental business?



**APPLY**

29. **Make Sense and Persevere** The radius of a sphere can be found using the function  $r = \sqrt[3]{\frac{3V}{4\pi}}$ , where  $V$  is the volume of the sphere. Heather filled a basketball with 448.92 in.<sup>3</sup> of air.



- Graph the function.
  - Identify the domain and range of the graph.
  - Do the domain and range make sense in this context? Explain.
  - What is the length of the radius of the basketball?
30. A formula for calculating the distance to the horizon is  $d = \sqrt{\frac{h}{0.57}}$ , where  $d$  is the distance to the horizon, in miles, and  $h$  is the height above the surface, in feet.



- Graph the function.
- Reason** What is your height above the surface if you can see a distance of 5 mi to the horizon?

**ASSESSMENT PRACTICE**

31. Choose yes or no to tell whether the function is an odd function.
- $f(x) = 5\sqrt{x - 10} - 12$      Yes     No
  - $f(x) = \frac{1}{4}\sqrt[3]{x}$      Yes     No
  - $f(x) = \frac{1}{2}\sqrt{x + 8} - 1$      Yes     No
  - $f(x) = 6\sqrt[3]{x}$      Yes     No
  - $f(x) = 9\sqrt[3]{x - 7} + 8$      Yes     No
32. **SAT/ACT** Which function has a graph with domain  $x \geq -1$  and range  $y \geq -2$ ?
- Ⓐ  $f(x) = \sqrt{x - 1} + 2$     Ⓑ  $f(x) = \sqrt[3]{x + 1} - 2$   
 Ⓒ  $f(x) = \sqrt[3]{x - 1} + 2$     Ⓓ  $f(x) = \sqrt{x + 1} - 2$
33. **Performance Task** The table shows the domain and range of the function  $f(x) = \sqrt[n]{x}$  for different values of  $n$ , where  $x$  is a positive real number.

$n$	Domain of $f(x) = \sqrt[n]{x}$	Range of $f(x) = \sqrt[n]{x}$
1	All real numbers	All real numbers
2	$x \geq 0$	$y \geq 0$
3	All real numbers	All real numbers
4		
5		
6		
7		
8		

**Part A** Identify the domain and range of the function  $f(x) = \sqrt[n]{x}$  when  $n = 4, 5, 6, 7,$  and  $8$ .

**Part B** Make a conjecture about the values of  $n$  that gives a domain and range of all real numbers.

**Part C** Make a conjecture about the values of  $n$  that gives a domain of  $x \geq 0$  and a range of  $y \geq 0$ .