



## 6-4 Reteach to Build Understanding

### Logarithmic Functions

- All exponential functions of the form  $f(x) = b^x$  and logarithmic functions of the form  $f(x) = \log_b x$  are \_\_\_\_\_, because these functions have exactly one  $y$ -value for each \_\_\_\_\_, so when the  $x$  and  $y$  are \_\_\_\_\_, the inverses will also have \_\_\_\_\_  $x$ -value for each \_\_\_\_\_.
- Find and correct the error a student made when finding the inverse of the logarithmic function  $f(x) = \log_6(4x + 2) - 5$ .

$$y = \log_6(4x + 2) - 5 \quad \text{Write in } y = f(x) \text{ form.}$$

$$x = \log_6(4y + 2) - 5 \quad \text{Interchange } x \text{ and } y.$$

$$x + 5 = \log_6(4y + 2) \quad \text{Add 5 on each side.}$$

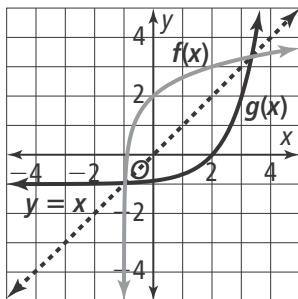
$$6^{x+5} = 4y + 2 \quad \text{Rewrite in exponent form.}$$

$$6^{x+3} = 4y \quad \text{Subtract 2 from each side.}$$

$$\frac{6^{x+3}}{4} = y \quad \text{Divide by 4 on each side.}$$

The equation of the inverse of  $f(x) = \log_6(4x + 2) - 5$  is  $f^{-1}(x) = \frac{6^x + 3}{4}$ .

- The  $f(x) = 3^{(x-2)} - 1$  and  $g(x) = \log_3(x + 1) + 2$  are inverse functions shown on the graph at the right. Complete the table without using a calculator.



$f(x) = 3^{(x-2)} - 1$		$g(x) = \log_3(x + 1) + 2$	
$x$	$y$	$x$	$y$
0	$-\frac{8}{9}$	$-\frac{8}{9}$	0
1	$-\frac{2}{3}$		
		0	2
3	2		
		8	4
5	26		
Domain:		Domain:	
Range: $\{y \mid y > -1\}$		Range: All real numbers	
$x$ -intercept: 2; $y$ -intercept: $-\frac{8}{9}$		$x$ -intercept: $-\frac{8}{9}$ ; $y$ -intercept: 2	
Asymptote:		Asymptote: $y = -1$	
End Behavior: As $x \rightarrow -\infty$ , $y \rightarrow -1$ As $x \rightarrow \infty$ , $y \rightarrow \infty$		End Behavior:	