## **PRACTICE & PROBLEM SOLVING**

Scan for Multimedia



#### UNDERSTAND

- 7. Use Structure Without applying the Change of Base Formula, explain how to use  $\log_3 2 \approx 0.631$  and  $\log_3 5 \approx 1.465$  to approximate  $\log_3(\frac{2}{5})$ .
- 8. Communicate Precisely Explain what is meant by expanding a logarithmic expression. How are the processes of expanding logarithmic expressions and writing logarithmic expressions as a single logarithm related?
- **9. Higher Order Thinking** The graph of  $y = \log(\frac{1}{x})$  and  $y = -\log x$  are shown. Notice the graph is the same for both equations. Use properties of logarithms to explain why the graphs are the same.



- **10.** Communicate Precisely Emma used the Change of Base Formula to solve the equation  $6^x = 72$  and found that x = 2.387. How can Emma check her solution?
- **11. Error Analysis** Describe and correct the error a student made in writing the logarithmic expression in terms of a single logarithm.

$$\log_3 2 + \frac{1}{2}\log_3 y = \log_3 2y^2$$

**12.** Error Analysis A student wants to approximate  $\log_2 9$  with her calculator. She enters the equivalent expression  $\frac{\ln 2}{\ln 9}$ , but the decimal value is not close to her estimate of 3. What happened?

$$\log_2 9 = \frac{\ln 2}{\ln 9}$$

PRACTICE

**13.** Use the properties of exponents to prove the Power Property of Logarithms. SEE EXAMPLE 1

Use the properties of logarithms to expand each expression. SEE EXAMPLE 2

<b>14.</b> $\log_5(\frac{2}{3})$	<b>15.</b> log <sub>6</sub> (2 <i>m</i> <sup>5</sup> <i>n</i> <sup>3</sup> )
<b>16.</b> ln 2x <sup>5</sup>	<b>17.</b> $\log_2\left(\frac{x}{5y}\right)$

Use the properties of logarithms to write each expression as a single logarithm. SEE EXAMPLE 3

**18.**  $9 \ln x - 6 \ln y$  **19.**  $\log_5 6 + \frac{1}{2} \log_5 y$ 

**20.**  $2\log 10 + 4\log (3x)$  **21.**  $\frac{1}{3}\ln 27 - 3\ln(2y)$ 

- **22.** 8log<sub>3</sub> 2 + 5log<sub>3</sub> c + 7log<sub>3</sub> d
- **23.** Use properties of logarithms to show that  $pH = log \frac{1}{[H^+]}$  can be written as  $pH = -log [H^+]$ . SEE EXAMPLE 4

Use the Change of Base Formula to evaluate each logarithm. Round to the nearest thousandth. SEE EXAMPLE 5

<b>24.</b> log <sub>4</sub> 9	<b>25.</b> log <sub>6</sub> 5
<b>26.</b> ln 3	<b>27.</b> log <sub>2</sub> 7
<b>28.</b> log <sub>9</sub> 12	<b>29.</b> ln 23

Use the Change of Base Formula to solve each equation for *x*. Give an exact solution as a logarithm and an approximate solution rounded to the nearest thousandth. SEE EXAMPLE 6

<b>30.</b> $3^{x} = 4$	<b>31.</b> 5 <sup><i>x</i></sup> = 11
<b>32.</b> 8 <sup><i>x</i></sup> = 10	<b>33.</b> 2 <sup><i>x</i></sup> = 30
<b>34.</b> 7 <sup><i>x</i></sup> = 100	<b>35.</b> 4 <sup><i>x</i></sup> = 55

# **PRACTICE & PROBLEM SOLVING**



### APPLY

36. Make Sense and Persevere The loudness of sound is measured in decibels. For a sound with intensity I (in watts per square meter), its loudness L(I) (in decibels) is modeled by the function  $L(I) = 10 \log \frac{I}{I_0}$ , where  $I_0$  represents the intensity of a barely audible sound (approximately  $10^{-12}$  watts per square meter).



- a. Find the decibel level of the sound made by the heavy traffic.
- b. Find the intensity of the sound that is made by music playing at 40 decibels.
- c. How many times as great is the intensity of the traffic than the intensity of the music?
- 37. Model with Mathematics Miguel collected data on the attendance at an amusement park and the daily high temperature. He found that the model  $A = 2 \log t + \log 5$  approximated the attendance A, in thousands of people, at the amusement park, when the daily high temperature is t degrees Fahrenheit.
  - a. Use properties of logarithms to simplify Miguel's formula.
  - b. The daily high temperatures for the week are below.





#### **ASSESSMENT PRACTICE**

38. Match each expression with an equivalent expression.

I.	log <sub>4</sub> 20	$\textcircled{A} \log_2 20 - \log_2 4$
II.	2log <sub>2</sub> 5	$(B) \log_4 2 + \log_4 10$
III. VI.	log <sub>2</sub> 5 4log <sub>4</sub> 2	

**39. SAT/ACT** Use the properties of logarithms to write the following expression in terms of a single logarithm.

$$2(\log_3 20 - \log_3 4) + 0.5 \log_3 4$$

- $(A) \log_3 4$ B log<sub>3</sub>5 © log<sub>3</sub>25 D log<sub>3</sub>50
- 40. Performance Task The magnitude, or intensity, of an earthquake is measured on the Richter scale. For an earthquake where the amplitude of its seismographic trace is A, its magnitude is modeled by the function:

$$R(A) = \log_{\frac{A}{A_0}},$$

where  $A_0$  represents the amplitude of the smallest detectable earthquake.

Part A An earthquake occurs with an amplitude 200 times greater than the amplitude of the smallest detectable earthquake,  $A_0$ . What is the magnitude of this earthquake on the Richter scale?

Part B Approximately how many times as great is the amplitude of an earthquake measuring 6.8 on the Richter scale than the amplitude of an earthquake measuring 5.9 on the **Richter scale?** 

Part C Suppose the intensity of one earthquake is 150 times as great as that of another. How much greater is the magnitude of the more intense earthquake than the less intense earthquake?